TFY4240

Problem set 5 Autumn 2015



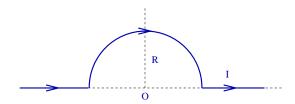
Problem 1.

Consider an infinitesimal static magnetic dipole of magnetic dipole moment m. In a coordinate system centered at the dipole, the vector potential associated with the dipole can in the Coulomb gauge be written

$$\mathbf{A}(\mathbf{r}) = \frac{\mu_0}{4\pi} \frac{\mathbf{m} \times \hat{\mathbf{r}}}{r^2}.$$
 (1)

- a) Use expression (1) to obtain an expression for the magnetic field B(r). Express your answer in *coordinate-free form*.
- **b)** Compare your answer from the previous subproblem with the expression for the electric field from a static electric dipole.

Problem 2.



An infinitely long wire carries a (time-independent) current I. The wire is bent so as to have a semi-circular detour, of radius R, around the origin O (see figure).

- a) Derive an expression for the magnetic field **B** at the origin O of the coordinate system.
- b) Determine the numeric value of this magnetic field given the current I=1 A and radius R=1 cm.

Problem 3.

Examples 6.1 and 6.3 from Griffiths.